

Activity 6

Extracts from Practice paper 4

Make a plan for doing these questions.

Write down the key idea(s) and then the mathematical processes that need to be done to make a successful attempt.

2. (a) Express $\frac{1}{(2x+3)(3x+2)}$ in partial fractions. (3)

(b) Hence find, in the form $y = f(x)$, the general solution of the differential equation

$$(2x+3)(3x+2)\frac{dy}{dx} = 5y \quad x > 0, y > 0 \quad (5)$$

3. Using the substitution $u = 1 + \tan x$, find the exact value of

$$\int_0^{\frac{\pi}{3}} \frac{1}{\cos^2 x + \sin x \cos x} dx \quad (6)$$

4.

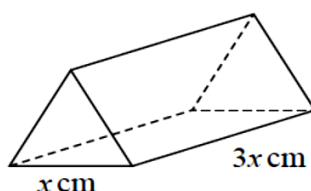


Figure 1

Figure 1 shows a right triangular prism. The cross-section is an equilateral triangle with side x cm and the length of the prism is $3x$ cm, with $x > 2$

Given that the cross-sectional area of the prism is changing at a rate of $(2 - x) \text{ cm}^2 \text{ s}^{-1}$

- (a) find, in terms of x , an expression for $\frac{dx}{dt}$ (4)

- (b) find the rate of decrease of the volume of the prism when $x = 2.05$ (4)